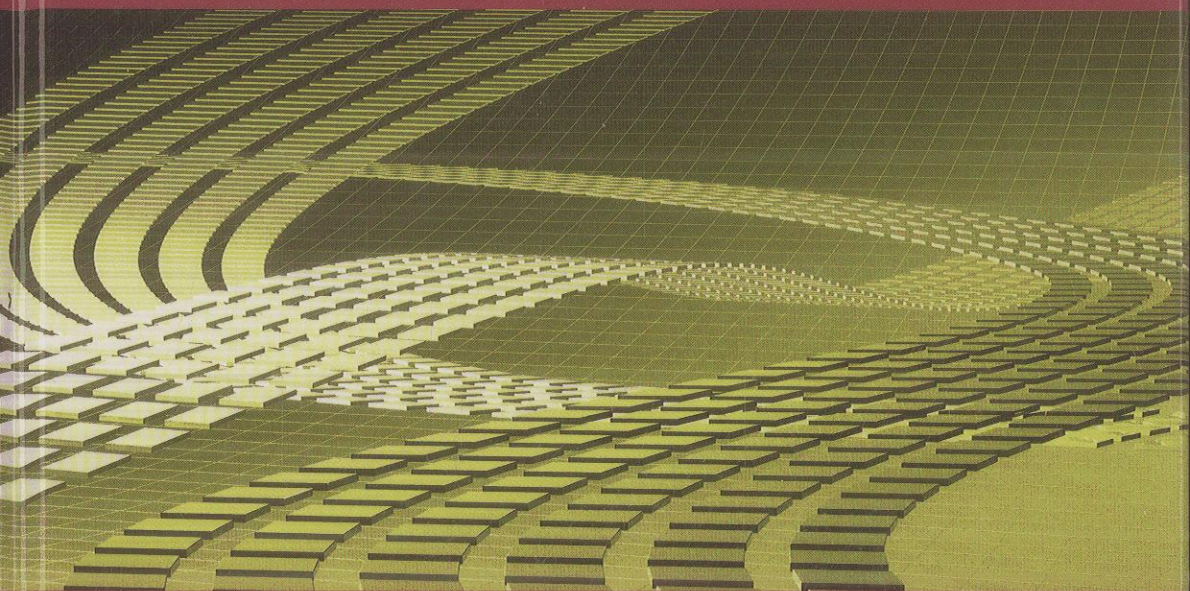


Mechanical Vibration and Shock Analysis



Fatigue Damage

Volume 4

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ISTE

 **WILEY**

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